Manuscript received: October 3th, 1994

GHTMDD - 237

UDC : 548. 75 : 541. 65 Original scientific paper

# INFRARED SPECTRA OF THE SULFATE ION TRAPPED IN POTASSIUM SELENATE – A COMPARISON WITH SULFATE DOPED POTASSIUM CHROMATE<sup>\*</sup>

## Vladimir M. Petruševski<sup>1</sup> and William F. Sherman<sup>2</sup>

<sup>1</sup>Institut za hemija, PMF, Univerzitet "Sv. Kiril i Metodij", POB 162, 91001 Skopje, Macedonia <sup>2</sup>Department of Physics, King's College, Strand, London, WC2R 2LS, UK

The FT-IR spectra of SO<sub>4</sub> doped K<sub>2</sub>SeO<sub>4</sub> were recorded at room (RT) and liquid-nitrogen temperature (LNT). The sulfate ions occupy sites of  $C_s$  symmetry. This leads to a complete removal of the degeneracy of the *E* and  $F_s$  modes. Exactly nine bands originating from the internal <sup>2</sup>SO<sub>4</sub> vibrations were found at both RT and LNT. Bands due to <sup>3</sup>SO<sub>4</sub> species could also be detected for the  $\nu_3$  and  $\nu_4$  mode components. Nine (out of the ten possible) second order transitions of the S–O stretchings were precisely measured at LNT. The harmonic frequencies of the S–O stretchings were calculated. The comparison with the SO<sub>4</sub> doped K<sub>2</sub>CrO<sub>4</sub> shows that (i) the sulfate ions are more distorted in a selenate than in a chromate host lattice; (ii) the anharmonicity constants of the  $x_{13i}$  type are larger that those of the  $x_{3i3i}$  type (iii) the ratio  $x_{13i}/x_{3i3i}$  of the anharmonicity constants appears to be smaller in the case of selenate than in the case of chromate host probably, mechanical anharmonicity dominates over the electric one. The possible reasons for these findings are discussed.

Key words: IR spectra; doped crystals; isolated ions; sulfate ion distortion; harmonic frequencies; anharmonicity constants.

### INTRODUCTION

A number of crystals having the structure of  $\beta$ -K<sub>2</sub>SO<sub>4</sub> are known: K<sub>2</sub>SO<sub>4</sub>, K<sub>2</sub>SeO<sub>4</sub>, (NH<sub>4</sub>)<sub>2</sub>SO<sub>4</sub>, K<sub>2</sub>CrO<sub>4</sub>, K<sub>2</sub>MnO<sub>4</sub>, (NH<sub>4</sub>)<sub>2</sub>BeF<sub>4</sub>, Rb<sub>2</sub>SeO<sub>4</sub> etc. Most of these have been very extensively studied by both diffraction and spectroscopic methods. The structure refinements [1-6] reveal the great similarity between the compounds; they all crystallize in the orthorhombic space group Pnam, with four formula units in the crystal cell. All ions are situated on mirror planes. The tetrahedral anions are fairly regular. The oxygen (i.e. fluorine – in  $BeF_4$  compounds) atoms either participate in the hydrogen bonding as proton acceptors (in the case of NH<sub>4</sub> compounds) or are 'coordinated' to the univalent metal cations (K, Rb, Tl etc.). It might be interesting to mention that although  $(NH_4)_2SeO_4$ and  $(NH_4)_2 CrO_4$  crystallize in the monoclinic crystal system (space group C2/m), still their structure shows a number of similarities with the compounds of the  $\beta$ -K<sub>2</sub>SO<sub>4</sub> type (e.g. all ions in the structure are at symmetry planes etc. [7,8]).

The spectroscopic studies are also numerous [9–15]. Both IR (transmission and reflection) and Raman techniques were employed in the assignment of

the sulfate internal modes in  $K_2SO_4$  [9]. The LO and TO mode frequencies were measured and reported too. Much attention was also paid to the study of pressure/temperature induced phase transitions in  $(NH_4)_2SO_4$  [10–15].

Directly related to the present work are the studies of doped and mixed crystals, particularly those in which various polyatomic ions were 'isolated' in the host matrix [16–34]. Of special interest are those concerned with sulfate doped alkali halides [25–29] and  $SO_4$  ions 'isolated' in a related isostructural compound (selenate, chromate, manganate or ferrate) [30–34]. In the latter studies conventional grating instruments have been used, so the results were (with a few exceptions) limited to reporting the frequencies of the  $\nu_3(SO_4)$  and  $\nu_4(SO_4)$  mode components.

Some time ago we studied the FT–IR spectra of sulfate doped  $K_2CrO_4$  [35] at LNT. The high signal-tonoise ratio allowed us to measure accurately the fundamental as well as second-order transition frequencies and to calculate the anharmonicity constants and the harmonic frequencies for the antisymmetric stretching

Dedicated to the 20th anniversary of the Bulletin

 $SO_4$  vibrations. In this work a more thorough investigation of sulfate doped  $K_2SeO_4$  was done. The results are presented and compared with those for  $SO_4$  doped  $K_2CrO_4$  [35, 36].

### EXPERIMENTAL

Sulfate doped potassium selenate was prepared from  $K_2CO_3$  and  $H_2SeO_4$ . The selenic acid already contained a small amount of  $SO_4$  impurities (although both chemicals were declared as being of reagent grade purity). Sulfate enriched samples (mole ratio of about 5%) were used for the measurement of the weak  $\nu_1(SO_4)$  and  $\nu_2(SO_4)$  bands which were otherwise completely masked by the high frequency wings of the intense  $\nu_3(SeO_4)$  and  $\nu_4(SeO_4)$  mode. Sulfate doped  $K_2CrO_4$  was prepared from mixtures of  $K_2CrO_4$  and  $K_2SO_4$ . The spectra were recorded from KBr pellets on a Perkin Elmer 1720 FT-IR spectrometer. The spectral resolution was about 1 cm<sup>-1</sup>. In order to have high quality spectra (high signal-to-noise ratio) one thousand spectra were accumulated. For sharp bands the measured frequencies are accurate to within 0.2– 0.3 cm<sup>-1</sup>. The integrated band intensities (I) were estimated as a product of the full width at half-maximum intensity (FWHMI =  $\Delta v_{1/2}$ ) and the absorbance (A) of the band. In order to sharpen the absorptions (reducing the number of 'hot' transitions, mainly two-phonon bands in which low frequency lattice phonons take place), low temperature studies were performed using a flow cryostat cooled with liquid nitrogen.

## RESULTS: GENERAL CONSIDERATIONS AND APPEARANCE OF THE SPECTRA

Initially, we shall briefly consider the spectra of  $\beta$ -K<sub>2</sub>SO<sub>4</sub>, in order to demonstrate the advantages of studying isolated ions, particularly ions which are subject to isomorphous isolation.

The LNT IR spectra of a KBr disk containing pure  $K_2SO_4$  are shown in Fig. 1. The application of group-theoretical methods (under the k = 0 approximation) reveals that two bands originating from  $\nu_1$ , three from  $\nu_2$  and five bands from both  $\nu_3$  and  $\nu_4$  are expected to appear in the powder IR spectra, as a consequence of both site-group and correlation-field splitting effects. Furthermore, in IR transmission studies (especially in ionic crystals, and in the vicinity of strong IR bands) the spectrum appears to be a result of superimposed transmission and reflection [37]. This is a consequence of the LO–TO splitting of the IR active modes (not predicted by the unit-cell group-theory approximation), leading to a high reflectivity of the sample in the frequency regions between  $\nu$ (TO) and  $\nu$ (LO) [38]. To summarize, a powder IR transmission spectrum is of relatively little value if one wishes to correlate the spectral and structural properties of the investigated material.

Things become even worse if one studies the second order transitions (two-phonon bands and true



Fig. 1. LNT IR spectra of a KBr disk containing pure  $K_2SO_4$  in the region of the  $SO_4$  stretching (a) and antisymmetric bending modes (b).

overtones) of pure  $K_2SO_4$ , in order to gain some knowledge of the anharmonicity of the  $SO_4$  stretching vibrations. The spectrum (cf. Fig. 2) is very rich, as a result of relaxation of the selection rules for multiphonon transitions. No band in this part of the spectrum could be simply assigned to a particular transition, as we discussed in our previous paper [35].



Fig. 2. LNT IR spectra of pure  $K_2SO_4$  in the region of second order transitions of the  $SO_4$  stretching modes

When sulfate ions are doped (at low concentration) in  $K_2SeO_4$  ( $K_2CrO_4$ ), they are more or less 'isolated'. This means that (i) interactions of identical oscillators (which cause Davydov splittings and the dispersion of phonon courves) and (ii) interactions (long-range electrostatic forces) leading to LO-TO splitting of the sulfate modes, can both be neglected. In such cases the number of bands (due to internal SO<sub>4</sub> vibrations) \* in the vibrational spectra and their activity may be predicted using site-group [39], rather than by ordinary unit cell-group analysis [40]. The results of these group theoretical considerations are given in Fig. 3. As a consequence of the  $C_s$  site symmetry, all degeneracies are removed and the forbidden  $v_1$  and  $v_2$  modes become allowed. The spectral picture of SO<sub>4</sub> doped K<sub>2</sub>SeO<sub>4</sub> at LNT (and also at RT) is in excellent agreement with these predictions, all nine bands being clearly detectable (Fig. 4). The frequencies of the components of  $v_3$  and  $v_4$  modes are in a good agreement with those reported by other authors [30–34], but  $v_1$  deviates by about 5 cm<sup>-1</sup> with respect to the value (985 cm<sup>-1</sup>) found by Hájek *et al.* [33]. As far as we know the components of the symmetric SO<sub>4</sub> bending have not been detected so far in this class of (isomorphous) solid solutions.

Some much weaker bands were found in the region of the  $\nu_3$  mode and one in the region of  $\nu_4$ . Three of them were assigned to vibrations of the  ${}^{34}SO_4$  species. In order to confirm this assignment, we made an approximate normal coordinate analysis for a 'free'  $SO_4$  ion and its  ${}^{34}SO_4$  and  $S{}^{18}O_4$  isotopomers. The GVFF method was employed [41]. The geometry of the sulfate ion (regular tetrahedron, R(S-O) = 147.2 pm) was taken from the work of Murray-Rust *et al.* [42]. The set of force constants used and the output results (vibrational frequencies) are presented in Table I.

The accumulation within the interferometer, of a great number of spectra allows even very weak bands to be detected, such as the overtones and combination bands of the components of the  $\nu_1$  and  $\nu_3$  modes.<sup>\*\*</sup> The corresponding region of the IR spectra is presented in Fig. 5.

Knowing the frequencies of both fundamental and second-order transitions allows one to calculate the anharmonicity constants [44]. The anharmonicity constant for the  $2\nu_1$  vibration was estimated from the IR spectrum of pure K<sub>2</sub>SO<sub>4</sub> (Fig. 2), taking the mean value of the unit-cell group components as the frequency of the  $\nu_1$  fundamental [36]. Previous studies [35]



Fig. 3. Correlation between the molecular point group and the site group of sulfate ions isolated in K2SeO4

The external modes of the sulfate ions absorb in the FIR region (below 200 cm<sup>-1</sup>) and will not be discussed in the present work.

Since the sulfate ions are *isolated* in the selenate matrix, and the frequencies of the  $SO_4$  stretching vibrations are well above all other (*i.e.*  $SeO_4$  stretching and/or bending) frequencies, terms *localized phonons* [43] or *localized vibrations* are often used. These are exponentially attenuated (rather than plane) waves. For simplicity the terms *fundamental mode* (vibration), *overtone* and *combination band* are used throughout the text, rather than *phonon*, *true overtone* and *two-phonon band* – which are more conveniently used in pure crystals.



Fig. 4. LNT IR spectra of SO<sub>4</sub> doped K<sub>2</sub>SeO<sub>4</sub>. (a)  $\nu_3$ (SO<sub>4</sub>); (b)  $\nu_1$ (SO<sub>4</sub>); (c)  $\nu_4$ (SO<sub>4</sub>) and (d)  $\nu_2$ (SO<sub>4</sub>) region

## Table I

Force constants and calculated frequencies for various  $SO_4$  isotopomers ( $f_{\alpha\alpha} = -f_{\alpha\alpha}$ ' was assumed [45])

Force constan	t Value/(N · cm <sup>-1</sup> )	Mode	<sup>32</sup> SO <sub>4</sub>	<sup>34</sup> SO <sub>4</sub>	<sup>32</sup> S <sup>18</sup> O <sub>4</sub>
			$\nu/\mathrm{cm}^{-1}$	$\nu/\mathrm{cm}^{-1}$	$\nu/\mathrm{cm}^{-1}$
$f_r$	7.263	ν <sub>1</sub>	983.0	983.0	926.8
f <sub>rr</sub>	0.614	$\nu_2$	450.1	450.1	424.3
$d^2 f_{\alpha}$	2.019	v <sub>3</sub>	1104.9	1088.7	1073.9
$d^2 f_{\alpha\alpha}$	0.2135	ν <sub>4</sub>	611.1	607.9	581.7
$d^2 f_{\alpha \alpha'}$	-0.2135				
$0d^2(f_{r\alpha} - f_{r\alpha'})$	) 0.340				

have shown that no bands attributable to combinations of stretching and bending modes could be found in the IR spectra, thus suggesting that the corresponding anharmonicity constants are negligibly small. Since the site symmetry of the sulfate ions is low, all degeneracies are removed, and equations for the non-degenerate case might be applied [44]. The calculation of the harmonic frequencies, is therefore, straightforward. All data are summarized in Table II. Data for  $SO_4$  doped  $K_2CrO_4$  are given for comparison in Table III. The calculated harmonic frequencies are given in Table IV.

Fig. 6 shows that there is a good correlation between the intensity of the second-order transitions and the corresponding values of the anharmonicity constants.

72



Fig. 5. LNT IR spectra of  $SO_4$  doped  $K_2SeO_4$  in the region of the second order transitions of the  $SO_4$  stretching modes

## Table II

Band frequencies, intensities and anharmonicity constants for  $SO_4$  ions doped in  $K_2SeO_4$ , at LNT and RT (primes refer to  ${}^{34}SO_4$  species).

billion	LNT			RT		
Mode	$\nu/cm^{-1}$	I/(arb. units	$x_{ij}^{\prime}/cm^{-1}$	$\nu$ /cm <sup>-1</sup>	$x_{ij}^{\prime}/cm^{-1}$	
$v_{2a}$	447.5 .	0.0011		447.5	816 661.68	
v <sub>2b</sub>	450.0	0.0019		451.5		
					C Startin	
$\nu_{4a}'$	610.0	Tastobe				
V <sub>4a</sub>	613.5	0.85		614.0	ie norma	
v <sub>4b</sub>	617.0	0.70		617.5	free Sta	
ν <sub>4c</sub>	623.0	0.62		622.5		
ν <sub>1</sub>	980.5	0.043		978.0	il), the	
v3a'	1089.5	0.031			nasilingi	
v <sub>3b</sub> '	1096.5	0.073			(,Os2)	
$\nu_{3a}$	1103.5	3.2		1104.5	nore quan	
???	1108.3	022106649				
may be					wishes h	
V <sub>3b</sub>	1115.5	4.3		1114.0		
v <sub>3c</sub>	1127.1	-				
v <sub>3c</sub>	1142.0	4.5		1139.5	TEL .	
$2\nu_1$	-	Later	-1.75*			
$v_1 + v_{3a}$	2073.0	0.033	-11.0	2074.5	-8.0	
$v_1 + v_{3b}$	2086.0	0.035	-10.0	2081.7	-10.3	
$v_1 + v_{3c}$	2113.0	0.034	-9.5	2110.5	-7.0	
$2\nu_{3a}$	2199.0	0.0045	-4.0			
$v_{3a} + v_{3b}$	2115.5	0.010	-3.5	2216.3	-2.2	
$2\nu_{3b}$	2224.3	0.0085	-3.35			
$v_{3a} + v_{3c}$	2245.5	0.0018	0.0			
$v_{3b} + v_{3c}$	2257.0	0.0022	-0.5			
$2\nu_{3c}$	2274.0	0.011	-5.0	2269.5	-4.75	



vs anharmonicity – a least-squares best-fit line

### Table III

LNT frequencies and anharmonicity constants for  $SO_4$  ions doped in  $K_2CrO_4$  [35, 36] (primes refer to  ${}^{34}SO_4$  species)

Mode	$\nu/\mathrm{cm}^{-1}$	x <sub>ij</sub> /cm <sup>-1</sup>
$\nu_{4a}$	612.0	r the relative splitting
ν <sub>4b</sub>	616.5	ALISTSIT ACCEPTING
v <sub>4c</sub>	622.5	6.
$\nu_1$	984.0	n tear anaeanan ryan Dasman hundaharay
ν <sub>3a</sub> '	1092.5	ns are only 'slightly' d
ν <sub>3b</sub> '	1099.5	
v <sub>3a</sub>	1106.5	
v <sub>3c</sub> '	1110.5	
ν <sub>3b</sub>	1117.5	
???	1127.5	
ν <sub>3c</sub>	1133.5	
$2\nu_1$		-1.75*
$\nu_1 + \nu_{3a}$	2075.0	-15.5
$\nu_1 + \nu_{3b}$	2087.0	-14.5
$v_1 + v_{3c}$	2104.0	-13.5
$2\nu_{3a}$	2205.0	-4.0
$v_{3a} + v_{3b}$	2220.0	-4.0
2v <sub>3b</sub>	2227,0	-4.0
$v_{3a} + v_{3c}$	2239.0	-1.0
$v_{3b} + v_{3c}$	2250.0	-1.0
2v <sub>3c</sub>	2258.0	-4.5

\*Estimated value (see text for details)

\*Estimated value (see text for details)

### Table IV

Harmonic frequencies (at LNT) for the stretching vibrations of  $SO_4$  ions doped in  $K_2SeO_4$  and  $K_2CrO_4$ 

K2S	eO4	K20	CrO <sub>4</sub>
Mode	$\nu/\mathrm{cm}^{-1}$	Mode	$\nu/\mathrm{cm}^{-1}$
$\omega_1$	999.25	$\omega_1$	1009.25
$\omega_{3a}$	1118.75	ω <sub>3a</sub>	1124.75
ω <sub>3b</sub>	1129.30	ω <sub>3b</sub>	1135.25
w <sub>3c</sub>	1157.50	w <sub>3c</sub>	1150.25

### DISCUSSION

According to Ross [45], the frequencies of the normal vibrations for a "free" SO<sub>4</sub> ion are 983 ( $\nu_1$ ), 450 ( $\nu_2$ ), 1105 ( $\nu_3$ ) and 611 cm<sup>-1</sup> ( $\nu_4$ ). When these values are compared with the frequencies (cf. Table II) of the nine fundamentals observed for the isolated ions, one may conclude that the symmetry of these ions deviates only slightly from the ideal  $T_d$  symmetry; the largest splitting of the  $\nu_3$  mode components at LNT is 38.5 cm<sup>-1</sup> which compared with the centro-frequency ( $\nu_c =$ 1120.3 cm<sup>-1</sup>) of the  $\nu_3$  mode gives  $\approx 3.5$  % as a value for the relative splitting of the antisymmetric stretching vibration. The relative splittings of the  $\nu_4$  (antisymmetric bending) and  $\nu_2$  (symmetric bending) modes are much less pronounced (~1.5 %, and 0.55 %, respectively), indicating that the effects of angular distortion are somewhat smaller than those caused by the bond length distortion. Both findings suggest that the sulfate ions are only 'slightly' distorted, this conclusion being further confirmed by the low intensity of the symmetric stretching and bending mode components (these modes are IR forbidden for ions with  $T_d$  symmetry).

Another estimate for the degree of distortion of the studied SO4 ions may be made on the basis of their geometry. The method of Baur [46] is widely used for that matter, although more involved methods are also known [47-49]. Assuming that the geometry of the isolated SO<sub>4</sub> ions is basically the same as in pure  $\beta$ -K<sub>2</sub>SO<sub>4</sub>, one may calculate the distortion indices [46] DI(SO), DI(OO) and DI(OSO), which are measures for the departure of the S-O distances, O · · · O separations and O-S-O angles, respectively, from their mean values. The values calculated on the basis of the structural data [1] give DI(SO) = 0.0034 and DI(OSO)= 0.0024. One should, then, conclude that both diffraction and spectroscopic results suggest that the sulfate ions are more distorted with respect to the S-O distances than with respect to the O-S-O angles.

However, it is questionable to what extent the results obtained by X-ray diffraction on pure substances are transferable to the *dopant ions* in mixed crystals. Usually, it is a priori assumed that the geometry of the

structural units (in this case sulfate ions) does not change significantly during isomorphous isolation [49]. This is, of course, only an approximation. It is known from the literature that some of the  $K \cdots O$ distances in  $K_2SeO_4$  are slightly shorter and other slightly longer than the corresponding distances in  $K_2CrO_4$  [1,4]. Assuming that the same holds for the  $K \cdots O$  separations built with the O atoms of the dopant  $SO_4$  ions, one would expect that the shorter  $K \cdots O$  contacts will induce additional lengthening of the somewhat longer S–O bonds and vice versa. So, it is not surprising that the  $SO_4$  ions doped in  $K_2SeO_4$ are *slightly more distorted* than those doped in  $K_2CrO_4$ , at least when S–O distances are taken into consideration.<sup>\*</sup>

The spectra of SO<sub>4</sub> doped K<sub>2</sub>SeO<sub>4</sub> and K<sub>2</sub>CrO<sub>4</sub> are in agreement with this assumption (cf. Table II and III), the relative splitting  $\Delta \nu / \nu_c$  for the  $\nu_3$  mode components of SO<sub>4</sub> doped K<sub>2</sub>CrO<sub>4</sub> being  $\approx 2.5 \%$ (significantly smaller than the splitting of SO<sub>4</sub> doped K<sub>2</sub>SeO<sub>4</sub>). With appropriate modifications (to make it more quantitative), this simple method may be used to quantify the distortion of a dopant polyatomic ion in a series of isomorphous host crystals, for which the approach of Baur [46] or any of the other approaches based on crystallographic data are not applicable.

Weak bands are usually found in the vicinity of the intense absorptions due to the components of  $\nu_3$ and  $\nu_4$  modes (cf. Fig. 4 and Table II). Some of them are, probably, combinations of the  $\nu_1$  mode with low-frequency lattice modes, as shown by Lewis and Sherman [28]. Another reason for the appearance of bands in this region is the existence of <sup>34</sup>SO<sub>4</sub> ions (the abundance of <sup>34</sup>S in the natural sulfur is about 4.3 %). An empirical assignment of these bands was made on the basis of their position; they are all 'shifted' to low wavenumbers, with respect to the corresponding <sup>32</sup>SO<sub>4</sub> bands.

In line with this, the comparison of the RT and LNT data (cf. Table I) also suggests that the  $SO_4$  ions are somewhat more distorted at LNT. This finding may be explained in terms of the unit cell contraction at low temperatures, the entities (ions) being packed more tightly. This may be expected to increase the order of the K···O 'bonds', resulting in a more distorted sulfate ion.

The calculations based on NCT (Table I) gave additional evidence that this assignment is correct (the results are in very good agreement with those obtained by Vojta and Koch [50]). It is important to note that the calculation suggests that larger 32S/34S shifts are expected for the components of the  $\nu_3$  mode than for those originating from  $\nu_4$  and this is what one really observes (cf. Table I). The appearance of only one band due to the  $\nu_4$ <sup>(34</sup>SO<sub>4</sub>) mode is not surprising; due to the small isotopic shifts ( $\approx 3 \text{ cm}^{-1}$ ) the other two components may be simply 'hidden' under the intense bands of  $\nu_{4}(^{32}SO_{4})$ . The IR spectra and the model calculations also suggest that the stretch-bend interaction force constants are not the same for all four S-O bonds; hence the slightly different isotopic ratios for the  $\nu_3$  mode-components.

Nine bands due to second-order transitions were clearly identified in the LNT IR spectra of the  $SO_4$  ions trapped in both  $K_2SeO_4$  and  $K_2CrO_4$  (Table II, Table III and Fig. 5). Only five such bands were resolved at RT (the bands at RT are significantly broader, partly due to the presence of 'hot bands', but also due to phonon collisions which reduce the mean-life of the excited states [51]). Due to insufficient data at RT, only the LNT spectra will be further discussed in more detail.

The anharmonicity constants of the type  $x_{3i3j}$  are several times smaller than those of the  $x_{13i}$  type. The reason for this seems to be clear : for sulfate ions which are only slightly distorted, the forms of the normal modes are expected to be close to those in 'free' SO<sub>4</sub> The symmetry coordinates of the following type (the  $r_i$ 's are the four S–O distances in the sulfate ion)

$$S_{1} = \frac{1}{2} (\Delta r_{1} + \Delta r_{2} + \Delta r_{3} + \Delta r_{4})$$

$$S_{3a} = \frac{1}{2} (\Delta r_{1} + \Delta r_{2} - \Delta r_{3} - \Delta r_{4})$$

$$S_{3b} = \frac{1}{2} (\Delta r_{1} - \Delta r_{2} + \Delta r_{3} - \Delta r_{4})$$

$$S_{3c} = \frac{1}{2} (\Delta r_{1} - \Delta r_{2} - \Delta r_{3} + \Delta r_{4})$$

5

may be used, to a first approximation, if one wishes to describe the four stretching vibrations. Now, for an ion with  $T_d$  symmetry the atomic displacements along  $S_{3i}$  and  $-S_{3i}$  are equivalent by symmetry (they are transformed into each other by the application of a suitable  $\hat{S}_4$  operation). As a consequence, all odd terms in the potential energy expansion of the  $\nu_3$  mode components vanish. For a slightly distorted sulfate ion, these terms are expected to be of much smaller value than the even ones. On the other hand, no symmetry operation transforms the displacement along  $S_1$  into  $-S_1$ , allowing cubic (as well as higher-order) terms to exist. Hence, the doubly excited  $\nu_3$  components are 'less anharmonic' compared to the combinations of  $\nu_1$  and  $\nu_3$ .

The ratio of the anharmonicity constants,  $x_{13i}/x_{3i3i}$ , might further be of interest. This ratio is, on

the average, somewhat bigger for the  $SO_4$  ions doped in  $K_2CrO_4$  than for  $SO_4$  doped  $K_2SeO_4$  (cf. Table III and Table II). In our previous paper [35] we predicted that this ratio is expected to have smaller value for more distorted sulfate ions and vice versa. It should be recalled that on the basis of the present investigation, the  $SO_4$  ions indeed seem to be slightly more distorted in the sulfate doped  $K_2SeO_4$  than in the corresponding chromate solid solution.

The calculated harmonic frequencies (cf. Table IV) for the stretching SO<sub>4</sub> frequencies of sulfate doped potassium selenate, are in good agreement with the results for sulfate doped potassium chromate [35]. In fact, in both cases the harmonic frequencies are equal within 10 cm<sup>-1</sup>.

Finally, the correlation found between the intensity of the second order transitions and the corresponding anharmonicity constants (Fig. 6) strongly suggests that the anharmonicity is predominantly mechanical in nature. In the dipole approximation, the intensity (*i.e.* transition moment) of an overtone transition is proportional to the square of the integral:

$$\langle \psi_i(\mathbf{q}) | q | \psi_{i+2}(\mathbf{q}) \rangle$$

where  $\varphi_i(\mathbf{q})$  are the true ('anharmonic') wave functions of an arbitrary mode. In principal, similar expressions may be written for the transition probability of a combination vibration. In accordance with the condition of completeness the wave functions may be expanded as a series of harmonic-oscillator eigenfunctions  $\phi_i(\mathbf{q})$ :

$$\psi_i(\mathbf{q}) = \sum_{j=0}^{\infty} c_{ij} \phi_j(\mathbf{q})$$

The  $c_{ij}$  coefficients for which i = j, are the basic terms in the expansion; all other terms appear due to the anharmonicity present. It is (at least intuitively) clear that the larger the anharmonicity, the larger will be the coefficients  $c_{ij}$  ( $i \neq j$ ), and consequently, the larger is the intensity of the second order transition. This, naturally, produces a correlation (although not necessarily a linear one). If, on the other hand, large electrical anharmonicity was present (arising from non-linear terms in the dipole moment expansion) than the correlation in Fig. 6 would be a mere coincidence. One finds this assumption rather improbable, and consequently less satisfying.

Further work on sulfate doped  $SrCrO_4$ ,  $BaCrO_4$ and  $BaSeO_4$  is in progress.

### Acknowledgement

This work was sponsored by the British Council, within the framework of the ALIS link, and by the Ministry of Science of the Republic of Macedonia. The authors sincerely appreciate the financial support of these two institutions.

#### REFERENCES

- [1] J.A. McGinnety, Acta Crystallogr., B28, 2845 (1972).
- [2] E.O. Schlemper, W.C. Hamilton, J. Chem. Phys., 44, 4498 (1966).
- [3] G.J. Palenik, Inorg. Chem., 6, 507 (1967).
- [4] A. Kálmán, J.S. Stephens, D.W.J. Cruickshank, Acta Crystallogr., B26, 1451 (1970).
- [5] A. Garg, R.C. Srivastava, Acta Crystallogr., B35, 1429 (1979).
- [6] I. Takahashi, A. Onodera, Y. Shiozaki, Acta Crystallogr., C43, 179 (1987).
- [7] R.L. Carter, C. Koerntgen, T.N. Margulis, *Acta Crystallogr.*, B33, 592 (1977).
- [8] J.S. Stephens, D.W.J. Cruickshank, Acta Crystallogr., B26, 437 (1970).
- [9] F. Meserole, J.C. Decius, R.E. Carlson, Spectrochim. Acta, 30A, 2179 (1974).
- [10] Y.S. Jain, H.D. Bist, G.C. Upreti, *Chem. Phys. Lett.*, 22, 572 (1973).
- [11] S.F.A. Kettle, U.A. Jayasooriya, L.-J. Norrby, J. Phys. Chem., 88, 5971 (1984).
- [12] G. Salvador, W.F. Sherman, G.R. Wilkinson, J. Mol. Struct., 143, 55 (1986).
- [13] P.K. Bajpai, Y.S. Jain, J. Phys. C 20, 387 (1987).
- [14] S.B. Kwon, J.J. Kim, J. Phys.: Condens. Matter., 2, 10607 (1990).
- [15] P.K. Bajpai, Y.S. Jain, H.D. Bist, J. Raman Spectrosc., 21, 327 (1990).
- [16] W.C. Price, W.F. Sherman, G.R. Wilkinson, Spectrochim., Acta 16, 663 (1960).
- [17] J.C. Decius, J.L. Jacobson, W.F. Sherman, G.R. Wilkinson, J. Chem. Phys., 43, 2180 (1965).
- [18] W.E. Klee, Spectrochim. Acta, 26A, 1165 (1968).
- [19] W.F. Sherman, P.P. Smulovitch, J. Chem. Phys., 52, 5187 (1970).
- [20] А.В. Кроль, Н.В. Левичев, А.И. Рыскин, Физ. тверд. тела, 19, 781 (1977).
- [21] V. Srinivasan, C.K. Subramanian, P.S. Narayanan, Pramana, 21, 41 (1983).
- [22] J.J. Kim, W.F. Sherman, Phys. Rev., B36, 5651 (1987).
- [23] R. Frech, E. Kazanelli, J. Solid State Chem., 74, 256 (1988).
- [24] H.D. Lutz, E. Alici, Th. Kellersohn, J. Raman. Spectrosc., 21, 387 (1990).
- [25] J.C. Decius, E.H. Coker, G.L. Brenna, Spectrochim. Acta, 19, 1281 (1963).
- [26] J.C. Decius, Spectrochim. Acta, 21A, 15 (1965).

- [27] M.A. Cundill, W.F. Sherman, Phys. Rev., 168, 1007 (1968).
- [28] S. Lewis, W.F. Sherman, Spectrochim. Acta, A35, 613 (1979).
- [29] М.У. Белый, В.В. Бойко, И.Я. Кушниренко, Укр. физ. журн., 33, 199 (1988).
- [30] P. Tarte, G. Nizet, Spectrochim. Acta, 20, 503 (1964).
- [31] H.J. Becher, F. Friedrich, H. Willner, Z. annorg. allg. Chem., 395, 134 (1973).
- [32] Г.Е. Краснянский, П. Цященко, Физ. тверд. тела, 25, 2479 (1983).
- [33] B. Hájek, O. Smrčková, P. Záruba, Collect. Czechoslovak. Chem. Commun., 49, 1756 (1984).
- [34] G. Masetti, E. Campani, G.Gorini, *Indian J. Pure Appl. Phys.*, 26, 94 (1988).
- [35] V. Petruševski, W.F. Sherman, J. Mol. Struct., 219, 171 (1990).
- [36] V.M. Petruševski, W.F. Sherman, unpublished results.
- [37] P.M.A. Sherwood, Spectrochim. Acta, 27A, 1019 (1971).
- [38] J.C. Decius, R.M. Hexter, Molecular Vibrations in Crystals, McGraw Hill, New-York, 1977.
- [39] R.S. Halford, J. Chem. Phys. 14, 8 (1946).
- [40] W.G. Fateley, F.R. Dollish, N.T. McDevitt, F.F. Bentley, Infrared and Raman Selection Rules for Molecules and Lattice Vibrations: The Correlation Method, Wiley-Interscience, New York, 1972.
- [41] J.R. Ferraro, J.S. Ziomek, Introductory Group Theory, Plenum Press, New York, 1975.
- [42] P. Murray-Rust, H.B. Bürgi, J.D. Dunitz, Acta Crystallogr., B34, 1793 (1978).
- [43] P.M.A. Sherwood, Vibrational Spectroscopy of Solids, Cambridge University Press, Cambridge, 1972.
- [44] G. Herzberg, Molecular Spectra and Molecular Structure : II. Infrared and Raman Spectra of Polyatomic Molecules, Van Nostrand, New York, 1956.
- [45] S.D. Ross, Inorganic Infrared and Raman Spectra, McGraw-Hill, London, 1972.
- [46] W.H. Baur, Acta Crystallogr., B30, 1195 (1974).
- [47] W.A. Dollase, Acta Crystallogr., A30, 513 (1974).
- [48] P. Murray-Rust, H.B. Bürgi, J.D. Dunitz, Acta Crystallogr., B34, 1787 (1978).
- [49] V. Petruševski, K. Trenčevski, Croat. Chem. Acta, 59, 867 (1986).
- [50] G. Vojta, D. Koch, Z. Phys. Chem., (Leipzig) 225, 295 (1964).
- [51] S. Califano, Proceedengs of the XIth International Conference on Raman Spectroscopy, Plenary Lecture 11, 43 (1988).

#### Резиме

#### ИНФРАЦРВЕНИ СПЕКТРИ НА СУЛФАТНИ ЈОНИ КАКО ПРИМЕСИ ВО КАЛИУМСЕЛЕНАТ – СПОРЕДБА СО СУЛФАТНИ ЈОНИ ВО КАЛИУМ ХРОМАТ –

#### Владимир М. Петрушевски<sup>1</sup> и William F. Sherman<sup>2</sup>

<sup>1</sup>Институт за хемија, ПМФ, Универзитет "Св. Кирил и Методиј", п.ф. 162, 91001 Скопје, Македонија <sup>2</sup>Department of Physics, King's College, Strand, London, WC2R 2LS, UK

Клучни зборови: инфрацрвени спектри; кристали со примеси; изолирани јони; деформација на SO<sub>4</sub> јони; хармониски фреквенции; константи на анхармоничност.

Фуриетрансформни инфрацрвени спектри на калиум селенат онечистен со сулфатни јони се снимани на собна и на ниска температура. Сулфатните јони лежат на рамнини на симетрија. Како резултат на тоа доаѓа до потполно отстранување на дегенерацијата на нивоата од  $E \ M F_2$  симетриски тип. Во областа на внатрешните вибрации од  ${}^{32}SO_4$  групациите се најдени точно девет ленти. За  $\nu_3$  и  $\nu_4$  модовите, регистрирани се и ленти од  ${}^{34}SO_4$  изотопомерите. Прецизно се из- мерени спектралните параметри на девет (од вкупно 10) премини од втор ред, што се во врска со валентните S-O вибрации. Пресметани се и хармониските фреквенции на валентните модови. Споредбата со SO<sub>4</sub> "онечистен" K<sub>2</sub>CrO<sub>4</sub> покажува дека: (i) сулфатните јони се подеформирани во селенатна, отколку во хроматна матрица; (ii) константите на анхармоничност од  $x_{13i}$  тип се поголеми од оние од  $x_{3i3j}$  тип; (iii) односот  $x_{13i}/x_{3i3j}$  е помал за сулфатни јони вградени во селенатна матрица; (iv) најверојатно, е доминантна механичка анхармоничност на вибрациите. Дискутирани се можните причини за овие наоди.